

## Model R.Sun for obtaining the daily global solar

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### ABSTRACT

The depletion of the conventional energy resources (fossil, oil and gas), pollution, and climate change require reflection on the need for energy diversification by a fast integration of renewable energies. The most important benefit of renewable energies is the solar energy, which is the main prerequisite of the life on the Earth. It is the direct source for generating heat, light, cold and power. Solar energy can be used in different ways, either in the photovoltaic systems for the electricity production or in thermal systems for the hot water production, field where it knows a considerable development particularly in the housing sector.

In this paper we will determine the empirical model R.sun that will allow us to estimate the daily global radiation on a horizontal plane and compare with the results measured at the site of Adrar city of Algeria when four seasons.

The expected results of this comparison are of importance for the investment study of solar systems (solar power plants for electricity production, for example) and also for the design and performance analysis of any system using the solar energy.

**Key words:** Solar radiation, Adrar, R.Sun, Irradiation.

### NOMENCLATURE

G<sub>hc</sub>: Global radiation (W/m<sup>2</sup>)  
 I<sub>N</sub>: Direct radiation (W/m<sup>2</sup>)  
 D<sub>hc</sub>: Diffuse radiation (W/m<sup>2</sup>)  
 I<sub>0</sub>: Solar constant (W/m<sup>2</sup>)  
 T<sub>L</sub>: Atmospheric disturbance factor linke  
 δ<sub>R</sub>: Rayleigh optical thickness  
 T<sub>a</sub>: Transmission factor  
 F<sub>d</sub>: Diffuse Function  
 γ: Height of the sun  
 θ: Latitude (°)  
 δ: Declination (°)  
 TSV: True solar  
 J: Day number in years

### 1. INTRODUCTION

The Algeria potential for renewable energy is strongly dominated by solar energy. Algeria considers this source of energy as an opportunity and a lever for economic and social development, particularly through the establishment of wealth and job-creating industries. The potential for wind,

biomass, geothermal and hydropower energies is comparatively very small. This does not, however,

preclude the launch of several wind farm development projects and the implementation of experimental projects in biomass and geothermal energy [5].

Global energy demand is growing rapidly, and natural energy resources such as oil, gas and uranium decrease due to a large dissemination and development of the industry in recent years. To cover the energy needs, research is conducted in renewable energy. A renewable energy that can fulfill the demand of the world until now, solar energy is free and inexhaustible in most parts of the world and has become an economic source [10].

Knowledge of solar radiation and these components on horizontal and inclined surfaces is necessary and indispensable to any study or design of solar installations. But generally, in the meteorological stations the global solar radiation is measured on horizontal surfaces and on the capital of each region [11].

The monitoring stations are rare across the country. For the estimation of the solar radiation, we use theoretical models. These models are built in the form of correlation. In order to be applicable to sites considered, they must be confronted with the actual measured values on the site considered over a period covering the deferent seasons [12].

However, a comparative study was performed on solar illumination on a horizontal plane. Do this several days were selected to compare the values calculated by this model and those given by the radiometric station of Adrar. We chose the site of Adrar to the study, the choice of this site was made on the availability of radiometric data sought. Indeed, Adrar is a Saharan town in the middle of the Sahara, this region known by very high daytime temperatures in summer and low temperatures in winter shows Figure 1. The experimental data of solar radiation used in 2014 came from Research Unit in Renewable Energies in the Saharan Medium in Adrar (URER-MS).

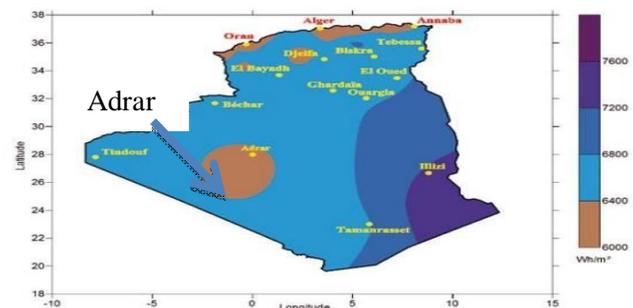
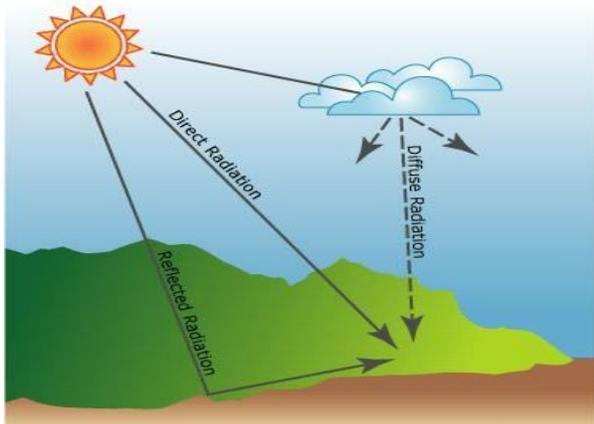


Figure 1: Monthly average of solar irradiation of Algeria [6]

## 2. MODEL DESCRIPTION

A modeling of the solar radiation will be presented according to the mathematical R.sun model. This model use specific equation for the determination of the geometrical parameters (solar declination angle, height of the sun, azimuth and angle of incidence....etc.) and atmospheric parameters (optical thickness of the atmosphere and Linke turbidity factor).

The global radiation received is the sum of direct radiation, diffuse and reflected components, Figure 2 shows the components of the solar radiation [7].



**Figure 2:** Components of the global radiation

### 2.1. R. Sun model

The direct normal radiation is expressed as a function of the factor  $T_L$  using the formula:

$$I_N = I_0 \exp(-T_L m \delta_R) \quad (1)$$

The beam irradiance normal to the solar beam  $B_{0c}$  ( $W/m^2$ ), attenuated by the cloudless atmosphere, is calculated as follows [1]:

$$B_{0c} = G_0 \exp\{-0.8662 T_{LK} m \delta_R(m)\} \quad (2)$$

The term  $-0.8662 T_{LK}$  is the air mass 2 Linke atmospheric turbidity factor [2]. The parameter  $m$  refer in (1) is the relative optical air mass calculated using the formula [1]:

$$m = (p/p_0)/(\sin h^{ref} + 0.50572 (h^{ref} + 6.07995) - 1.6364) \quad (3)$$

where  $h^{ref}$  is the corrected solar altitude  $h$  (an angle between the sun and horizon) in degrees by the atmospheric refraction component  $\Delta h^{ref}$ :

$$\Delta h^{ref} = 0.061359 (0.1594 + 1.123 h + 0.065656 h^2) / (1 + 28.9344 h + 277.3971 h^2) \quad (4)$$

$$h^{ref} = h + \Delta h^{ref} \quad (5)$$

The  $p/p_0$  component in (3) is correction for given elevation  $\gamma$  (m):

The parameter  $\delta_R(m)$  in (1) is the Rayleigh optical thickness at air mass  $m$  and is calculated according to the improved formula as follows [1]:

for  $m \leq 20$ :

$$\delta_R(m) = 1 / (6.6296 + 1.7513 m - 0.1202 m^2 + 0.0065 m^3 - 0.00013 m^4) \quad (7)$$

for  $m > 20$

$$\delta_R(m) = 1 / (10.4 + 0.718 m) \quad (8)$$

The beam irradiance on a horizontal surface  $B_{hc}$  ( $W/m^2$ ) is then calculated as:

$$B_{hc} = B_{0c} \sin h \quad (9)$$

The beam irradiance on an inclined surface  $B_{ic}$  ( $W/m^2$ ) is calculated as:

$$B_{ic} = B_{0c} \sin \delta_{exp} \quad (10)$$

Or

$$B_{ic} = B_{hc} \sin \delta_{exp} / \sin h \quad (11)$$

Where  $\delta_{exp}$  is the solar incidence angle measured between the sun and an inclined surface defined in (12).

In the R.sun model we have implemented the sun declination  $\delta$  (rad) defined as [1]:

$$\delta = \arcsin(0.3978 \sin(j' - 1.4 + 0.0355 \sin(j' - 0.0489))) \quad (12)$$

$$p/p_0 = \exp(-\gamma/8434.5) \quad (6)$$

As the cloudless sky becomes more turbid, the diffuse irradiance increases, while the beam irradiance decreases. The estimate of the diffuse component on a horizontal surface  $D_{hc}$  ( $W/m^2$ ) is made as a product of the normal extraterrestrial irradiance  $G_0$ , a diffuse transmission function  $T_n$  dependent only on the Linke turbidity factor  $T_{LK}$ , and a diffuse solar altitude function  $F_d$  dependent only on the solar altitude  $h$  [1],[3]:

$$D_{hc} = G_0 T_n(T_{LK}) F_d(h) \quad (13)$$

The estimate of the transmission function  $T_n(T_{LK})$  gives a theoretical diffuse irradiance on a horizontal surface with the sun vertically overhead for the air mass 2 Linke turbidity factor. The following second order polynomial expression is used:

$$T_n(T_{LK}) = -0.015843 + 0.030543 T_{LK} + 0.0003797 T_{LK}^2 \quad (14)$$

The solar altitude function is evaluated using the expression:

$$F_d(h) = A_1 + A_2 \sin h + A_3 \sin^2 h \quad (15)$$

where the values of the coefficients A1, A2 and A3 are only depended on the Linke turbidity factor  $T_{LK}$  defined in the following expressions:

$$A_1' = 0.26463 - 0.061581 T_{LK} + 0.0031408 T_{LK}^2 \quad (16)$$

$$A1 = 0.0022/T_n(T_{LK}) \quad \text{if } A1' T_n(T_{LK}) < 0.0022 \quad (17)$$

$$A1 = A_1' \quad \text{if } A1' T_n(T_{LK}) \geq 0.0022 \quad (18)$$

$$A2 = 2.04020 + 0.018945 T_{LK} - 0.011161 T_{LK}^2 \quad (19)$$

$$A3 = -1.3025 + 0.039231 T_{LK} + 0.0085079 T_{LK}^2 \quad (20)$$

The model for estimating the clear-sky diffuse irradiance on an inclined surface  $D_{ic}$  ( $W/m^2$ ) [4] distinguishes between sunlit, potentially sunlit and shadowed surfaces. The equations are as follows:

for sunlit surfaces and non-overcast sky (h in radians):

if  $h \geq 0.1$  (i.e.  $5.7^\circ$ )

$$D_{ic} = D_{hc} \{F(\gamma_N) (1 - K_b) + K_b \sin \delta \exp/\sin h\} \quad (21)$$

if  $h < 0.1$  (i.e.  $5.7^\circ$ )

$$D_{ic} = D_{hc} \{F(\gamma_N) (1 - K_b) + K_b \sin \gamma_N \cos A_{LN}/(0.1 - 0.008 h)\} \quad (22)$$

Where

$A_{LN}$  is the azimuth of the sun to an inclined surface.

$F(\gamma_N)$  is a function accounting for the diffuse sky irradiance.

The  $K_b$  is a measure of the amount of beam irradiance available (proportion between beam irradiance and extraterrestrial solar irradiance on a horizontal surface):

$$K_b = B_{hc}/G_{0h} \quad (23)$$

where  $G_{0h}$  ( $W/m^2$ ) is calculated as:

$$G_{0h} = I_0 \sin h \quad (24)$$

The global irradiance  $G$  ( $w/m^2$ ) on a horizontal surface can be given by:

$$G = I_N + D_{hc} \quad (25)$$



Figure 3: Used meteorological station Neal

### 3. RESULTS AND INTERPRETATIONS

#### 3.1 Achievements

For a validation of solar radiation, we will confront some values; clear sky, solar radiation provided by the radiometric station Adrar with values on the horizontal plane.

We present the following figures; comparative graphs relating to global radiation R.Sun model with experimental data of 2014 of the site Adrar. The relative error graph over time (TSV) is also given to the global radiation.

The expression of the average relative error (%) is given by the following equation:

$$Err = \frac{|G_{measured} - G_{calculated}|}{G_{measured}} \quad (26)$$

G: solar illumination ( $W/m^2$ )

#### 3.2. Results achieved for the day 22-03-2014

URER-MS Adrar

The experimental data on the components of global solar radiation on the horizontal plane, and a clear sky and a winter day on the town of Adrar are presented in figures below as graphs, and by comparing them with data from the model studied.

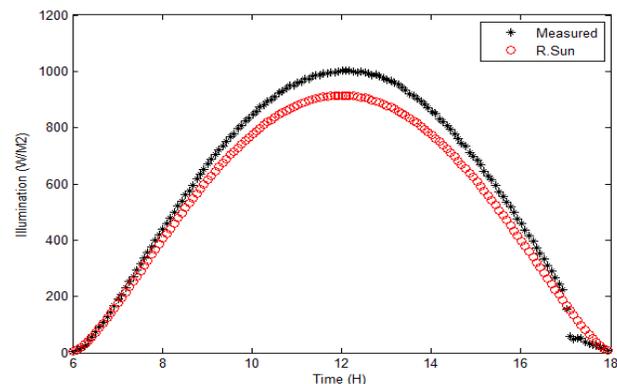


Figure 4: Global Illumination

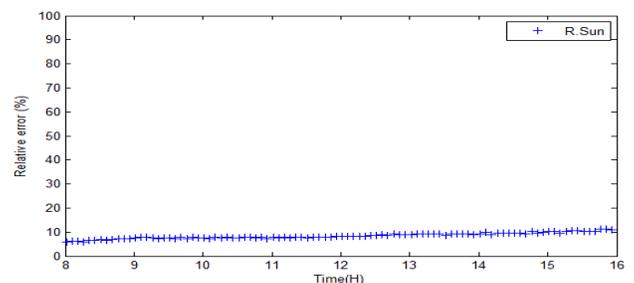


Figure 5: Instantaneous relative error

3.3. Results achieved for the day of 29-07-2014

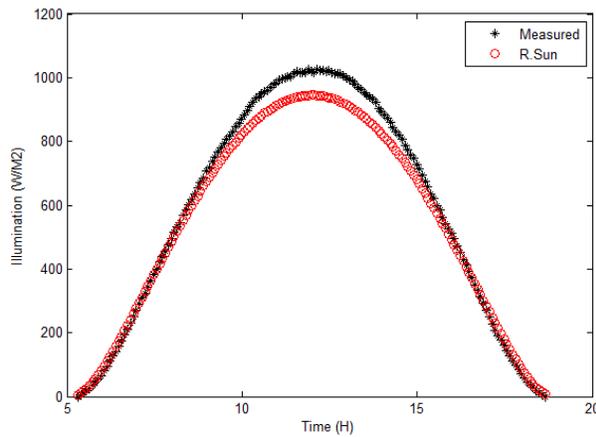


Figure 6: Global Illumination

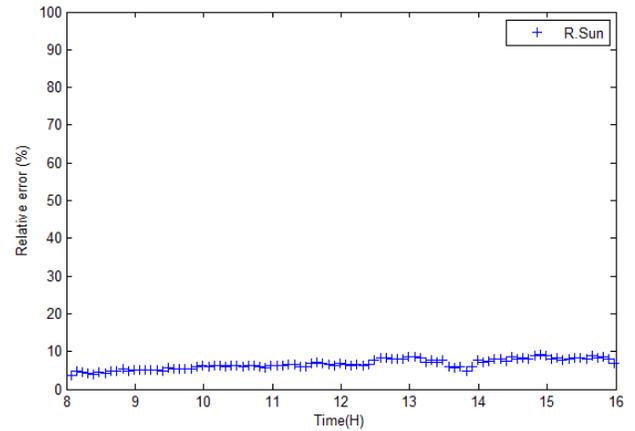


Figure 9: Instantaneous relative error

3.5. Results achieved for the day of 16-12-2014

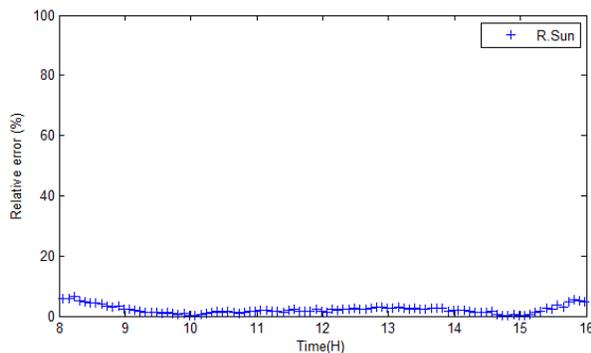


Figure 7: Instantaneous relative error

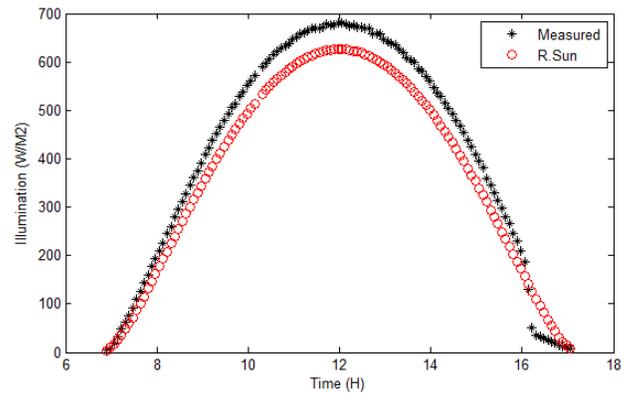


Figure 10: Global Illumination

3.4. Results achieved for the day of 13-09-2014

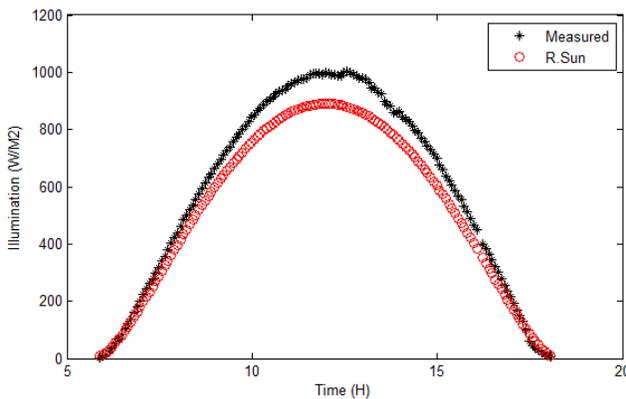


Figure 8: Global Illumination

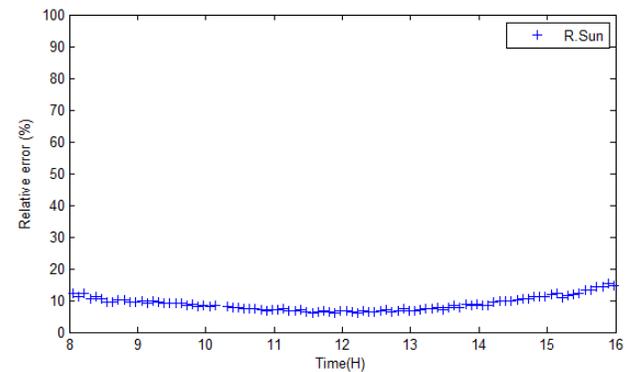


Figure 11: Instantaneous relative error

3.6. Comparative study and critical analysis

In order to achieve a critical analysis of the results, it was made a comparison of experimental data with those from the model. It was thus also calculated the relative error of global radiation at the site of Adrar.

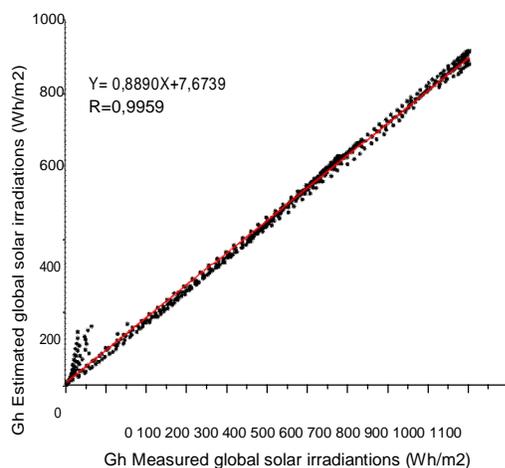
The results obtained are summarized in Table 2 below.

The average relative error is given by the following equation:

$$E_m (\%) = \sum_i \frac{Err(\%)}{i} \quad (27)$$

**Table 2:** Error calculation results on the horizontal sunlight for some clear days, on the site.

Day	Average relative error (%) R.Sun Model
22-03-2014	8,5845
29-07-2014	5.7376
13-09-2014	10.5202
16-12-2014	9.1771



**Figure 12:** Scatter plot of daily global solar radiation values estimated by R.Sun model vs. measured daily global solar radiation values.

#### 4. RESULTS AND INTERPRETATION

In analyzing the results shown in Figures (4 to 12) it is deduced that:

- The global solar radiation increases with the growth of time until a maximum value of about 12: 00 and then begins to decrease until it reaches zero (layer of the sun).
- We noticed that the solar flux varies around 1000 (W/ m<sup>2</sup>), with an increase in June and August, a slight decrease during the months of September and March and a considerable decline in December. This variation is mainly due to the declination angle and temperature change.
- This model is generally more favorable for estimating solar irradiance on a horizontal sensor especially in the month of July.
- For this model, note that for most situations, the values of the estimated global component are close to the measured values, the average relative error is small. A typical example appears July 29 where the curve simulated by the model are

- We also found this model is most beneficial during most seasons of the year (the error does not exceed 11% and the correlation 0.9959).

#### 5. CONCLUSION

In this article, modeling of solar radiation by the R.Sun model is presented and performed. Model used to own equations calculated atmospheric parameters (mass, optical thickness of the atmosphere....etc), and calculated the direct illumination, diffuse and global.

This work allowed us to compare the measured values and those estimated by the parameterized model. We found that the R.Sun model gives a good estimate of solar radiation (the error does not exceed 11% and the Correlation 0.9959). The results obtained for the site approach with great precision real data.

The R.Sun model is essential for estimating solar radiation horizontal (see Table 2), which is interesting to perform the dimensioning of thermal systems (hot water) and photovoltaic installations, particularly in Algeria. Because it is used more often than the horizontal solar radiation in the design of solar systems.

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