



Performance Evaluation of Multi-Layer Perceptron (MLP) and Radial Basis Function (RBF): COVID-19 Spread and Death Contributing Factors

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ABSTRACT

The Artificial Neural Network (ANN) is an Artificial Intelligence technique which has the ability to learn from experiences, enhancing its performance by adapting to the environmental changes. The key benefits of neural networks are the prospect of processing vast quantities of data effectively, and their ability to generalize outcomes. Considering the great potential of this technique, this paper aims to establish a performance evaluation of Multilayer Perceptron (MLP) and a Radial Basis Function (RBF) networks in investigating the contributing factors for COVID-19 spread and death. The RBF and MLP networks are typically used in the same form of applications, however, their internal calculation structures are different. A comparison was made by using a dataset of COVID-19 cases in 41 Asia countries during April 2020. There are nine contributing factors which acted as the covariates to the network such as Cases, Deaths, High Temperature, Low Temperature, Population, Percentage of Cases over Population, and Percentage of Death over Population, Average Temperature, and Total Cases. The results obtained from the testing sets indicated that the two neural structures were able to investigate the COVID-19 spread and death contributing factors. Nevertheless, the RBF network indicated a slightly better performance than the MLP.

Key words: COVID-19, Global Geographical Climate, Artificial Neural Network (ANN)

1. INTRODUCTION

COVID-19 has spread all over the world, locking up billions of people as health services struggle to cope [1]. Providentially, enormous global data distribution on COVID-19 is made available online with combination of global climate data, which creates an opening for further analysis to be conducted. This reflects the need for an analysis that is best suited to big data analysis which offers high performance and efficiency in understanding this pandemic issue.

The Artificial Neural Network (ANN) has the ability to learn from experiences, improving its performance and adapting to the changes in the environment [2]. The key benefits of neural networks are the prospect of processing vast quantities of data effectively, and their ability to generalize outcomes [3]. The ANNs are parallel distributed systems, consisting of simple processing units (artificial neurons) that measure with certain (usually nonlinear) [4] mathematical functions. These units are arranged in one or more layers and interconnected by a sufficient number of connections [5]. These connections are associated with weights in most models, which store the knowledge acquired by the model and are used to consider the input received by each neuron network [6].

The application of ANN to solve problems with fault diagnosis is of special interest due to its classification and practical approximation capabilities [7]. ANN approach is convenient when it is difficult to obtain an analytical model. There are numerous research conducted which using the ANN particularly on Multilayer Perceptron (MLP) and Radial Basis Function (RBF) such as and-written digit recognition [8], prediction of carbon dioxide solubility in ionic liquids [9], prediction of solution gas-oil ratio of crude oil systems [10], estimation of construction cost [11] and many more.

Considering the great potential of this technique, this paper aims to establish a comparison between a MLP and RBF in investigating the contributing factors for COVID-19 spread and death. The employment of the ANN is expected to contribute in understanding the contributing factors of the COVID-19 spread and death. The organization of the remainder of this paper is as follows: Section 2 elaborates the data background. Section 3 provides our methods, including an overview of the methodology, and the description of MLP and RBF structures. Our results and discussions are discussed in Section 4. Finally, in Section 5, we present our conclusion.

Table 1: Descriptive Statistics

		cases	deaths	HIGH TEMPERATURE	LOW TEMPERATURE	AVERAGE TEMPERATURE	population	TOTAL CASES	TOTAL DEATH	PERCENT CASES POPULATION	PERCENT DEATH POPULATION
N	Valid	41	41	41	41	41	41	41	41	41	41
	Missing	0	0	0	0	0	0	0	0	0	0
Mean		303.8537	8.5366	81.7756	63.9220	72.8756	111331860.0732	11519.7805	363.8293	.0094	.0002
Median		32.0000	.0000	88.7000	69.1000	79.3000	23816775.0000	6991.0000	165.0000	.0000	.0000
Mode		.00	.00	66.20 ^a	77.00	83.60 ^a	437479.00 ^a	4651.00 ^a	129.00 ^a	.00	.00
Std. Deviation		579.74393	21.18620	13.83014	14.11557	13.39953	303784756.30899	30617.90898	1238.19098	.05739	.00151
Variance		336103.028	448.855	191.273	199.249	179.547	92285178165.714976.0000	937456350.326	1533116.895	.003	.000
Skewness		3.010	2.989	-.785	-.836	-.751	4.090	6.376	6.388	6.376	6.366
Std. Error of Skewness		.369	.369	.369	.369	.369	.369	.369	.369	.369	.369
Kurtosis		10.588	8.308	-.341	-.134	-.433	16.218	40.762	40.869	40.757	40.666
Std. Error of Kurtosis		.724	.724	.724	.724	.724	.724	.724	.724	.724	.724
Range		2936.00	89.00	52.70	56.10	52.00	1438886297.00	199544.00	8032.00	.37	.01
Minimum		.00	.00	49.00	24.30	36.90	437479.00	2986.00	61.00	.00	.00
Maximum		2936.00	89.00	101.70	80.40	88.90	1439323776.00	202530.00	8093.00	.37	.01
Sum		12458.00	350.00	3352.80	2620.80	2987.90	4564606263.00	472311.00	14917.00	.39	.01
Percentiles	25	1.0000	.0000	72.1500	51.1000	60.6500	5478484.0000	5745.0000	135.5000	.0000	.0000
	50	32.0000	.0000	88.7000	69.1000	79.3000	23816775.0000	6991.0000	165.0000	.0000	.0000
	75	280.0000	4.5000	92.8500	76.0000	84.1000	76896463.5000	8344.5000	187.0000	.0000	.0000

2. DATA BACKGROUND

A COVID-19 dataset which includes the number of cases and death were collected from the European Centre for Disease Prevention and Control(ECDPC), global geographical climate data were taken from the Weather Forecast, and population data is obtained from the Current World Population. The dataset covered the 41 countries in Asia, however, due to incomplete data distribution, three countries were excluded which are Palestine, Tajikistan and Yemen. The descriptive statistics data can be seen in Table 1.

3. RESEARCH METHODS

This paper aims to establish a performance evaluation of MLP and a RBF against spread and death contributing factors for COVID-19. The description of the MLP and RBF structures are explained further in the next subsections.

3.1 Multilayer Perceptron (MLP) Network

The MLP was applied to various fields, performing tasks such as behavioral analysis [12], solar forecasting [13], and body weight estimation function fitting [14], using supervised

training with an algorithm called "error back propagation.". A basic neuron with R inputs is shown in Figure 1.

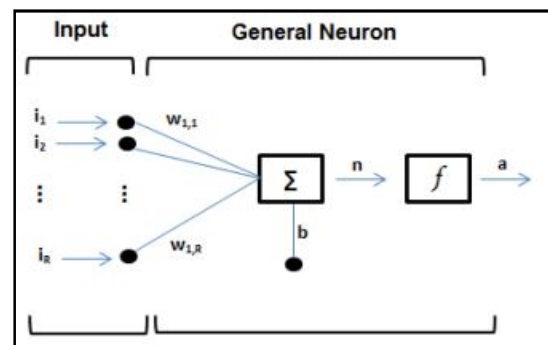


Figure 1: An elementary neuron with R inputs

Each input (*i*) is weighted with an appropriate *w*. The weighted inputs sum and the bias form the input to the activation function *f*, and (1) represents the appropriate mathematical expression.

$$a = f (w_i + b) \tag{1}$$

where:

a : output signal of the neuron

w : weights between the neurons

i : vector of input data

b : bias added to the neurons where each neuron in the network includes an activation function (f)

The MLP also has one or more hidden layers of sigmoid neurons, accompanied by a linear neuronal output layer. The most significant nonlinear activation functions for MLP are the logarithmic and hyperbolic tangent functions. The command for linear activation function is `purelin`. The nonlinear activation function multiple layers of neurons enable the network to learn nonlinear relationships between input and output vectors.

3.2 Radial Basis Function (RBF) Network

The RBF network has the advantages such as easy design consisting of three-layer architecture, good generalization and high input noise tolerance and online learning capabilities. From the point of generalization, RBF networks can respond well to patterns that were not used for training [15]. The RBF neural network has an input, hidden and output layer. The input layer consists of an input vector I , as shown in Figure 2.

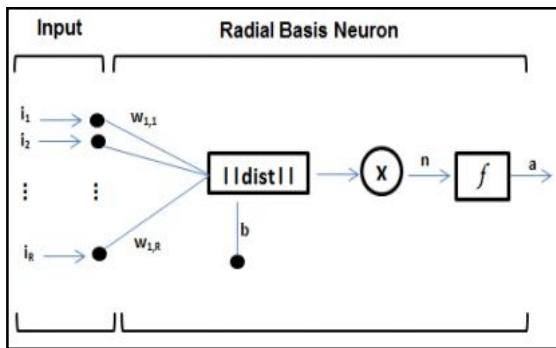


Figure 2: Radial basis network with R inputs

The networks neuron which is the RBF activation function is located in the hidden layer. The vector distance between its weight (w) and the input vector (i), multiplied by the bias b is the net input to the RBF activation function. The mathematical expression of one artificial neuron of a radial basis function network is shown in (2).

$$a = radbas (||w - i||b) \tag{2}$$

Radial functions are a special class of functions the value of which increases or decreases proportional to the distance from a central point. There are various types of radial basis functions, but the most commonly used is the Gaussian function. The command for using a RBF is `radbas`. The study in [16] claimed that the RBF networks are simpler than MLP networks. In spite of having more complex architectures, it is well known that the MLP networks have been applied successfully in several difficult problems. RBFs serve as local approximation networks and their outputs in certain local receptive fields are calculated by particular hidden units.

Oppositely, MLP networks run globally and all the neurons determine the network outputs.

4. RESULTS

The case processing summary for each MLP and RBF are presented in Table 2 and Table 3. In the preprocessing part, the data were divided into two sets which are training and testing. Based on the Table 2, the training set for MLP consist of 78% (32/41) of the overall data, while testing sets comprises of 21.95% (9/41) of the overall data, N=41. There were no excluded values recorded.

Table 2: MLP Case Processing Summary

		N	Percent
Sample	Training	32	78.0%
	Testing	9	22.0%
Valid		41	100.0%
Excluded		0	
Total		41	

On the other hand, the training set for RBF consist of 73.2% (30/41) of the overall data, while testing sets comprises of 26.8% (11/41) of the overall data, N=41. There were no excluded values recorded as well as depicted in Table 3.

Table 3: RBF Case Processing Summary

		N	Percent
Sample	Training	30	73.2%
	Testing	11	26.8%
Valid		41	100.0%
Excluded		0	
Total		41	

Subsequently, there are nine covariates used in the network which are Cases, Deaths, HighTemperature, Low Temperature, Population, Percentage of Cases over Population, and Percentage of Death over Population, Average Temperature, and Total Cases. These nine covariates were the inputs nodes in the input layer of the network. For the MLP, the network consists of only one hidden layer, with one single node. The activation function from input layer to hidden layer was Hyperbolic tangent. The target of the network is COVID-19 spread and death, where the activation function from hidden layer to output layer was identity (`purelin`). The default error function in backpropagation neural network was based on sum of squares (SSE). To simplify, the configurations of this network was 9-1-1. The network architecture for MLP can be referred in Figure 3.

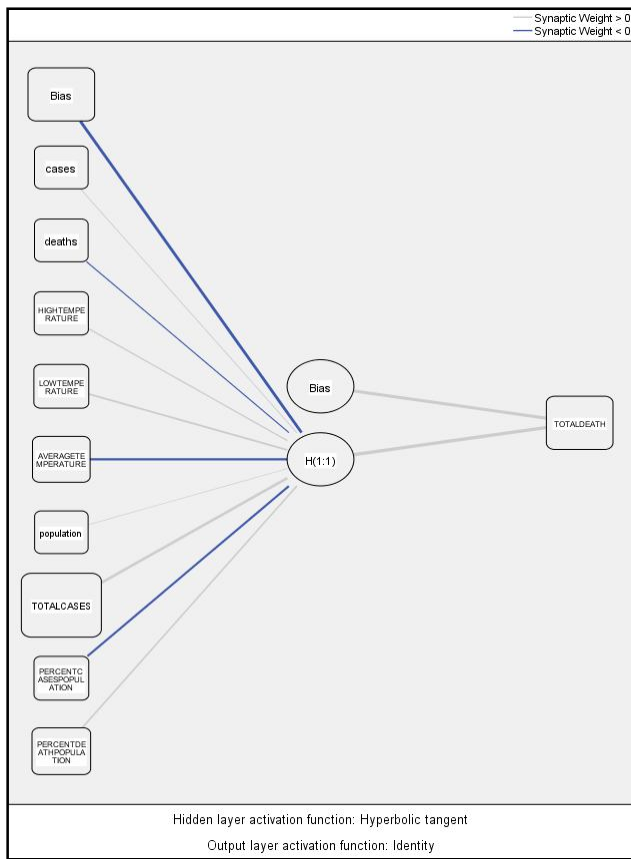


Figure 3: MLP Network Architecture

The RBF in contrast consists of seven hidden layers, with seven nodes. The activation function from input layer to hidden layer was Softmax. Similar to the MLP, the target of the network is COVID-19 spread and death, where the activation function from hidden layer to output layer was identity (purelin). The default error function in backpropagation neural network was based on sum of squares (SSE). To simplify, the configurations of this network was 9-7-1. The network architecture for RBF is illustrated in Figure 4.

Next, Table 4 depicts the model summary of both training and testing sets for MLP and RBF networks. The Sum of Squares Error (SSE) for the MLP is 0.012 and 0.005 for RBF in the training set, with Relative Error (RE) equals to 0.001 and 0.000 for MLP and RBF respectively. Conversely, the SSE for testing sets is 0.002 for MLP and 0.003 for RBF, with RE equals to 0.498 for MLP and 0.445 for RBF. It can be said that in any network, testing set should be the reference. The RE values for both MLP and RBF are monitored to be quite low. Therefore, it is firmly believed that both MLP and RBF network performances are in favorable structure.

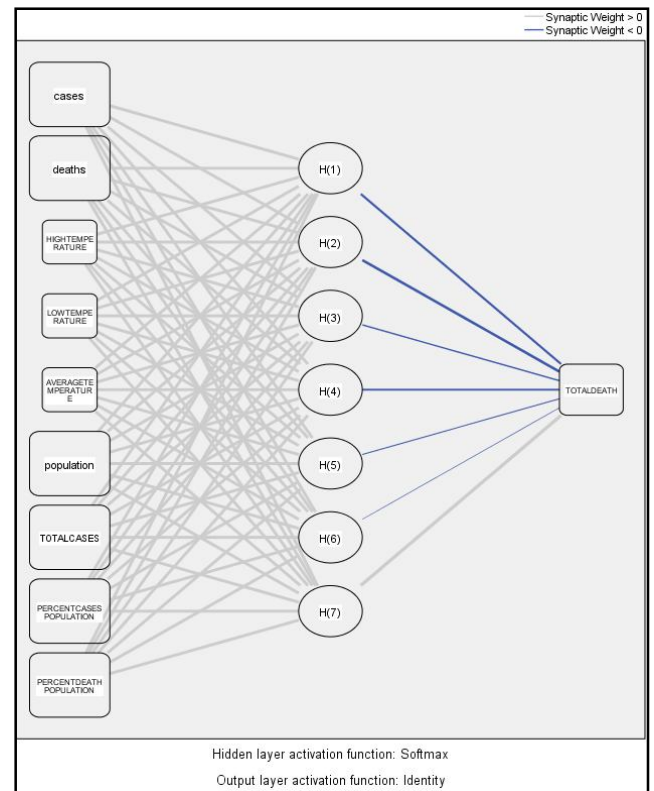


Figure 4: RBF Network Architecture

Table 4: MLP vs RBF Model Summary

		MLP	RBF
Training	Sum of Squares Error	.012	.005
	Relative Error	.001	.000
	Training Time	0:00:00.00	0:00:00.09
Testing	Sum of Squares Error	.002	.003 ^a
	Relative Error	.498	.445

Dependent Variable: TOTALDEATH

a. The number of hidden units is determined by the testing data criterion: The "best" number of hidden units is the one that yields the smallest error in the testing data.

Table 5 and Table 6 display the independent variable importance for MLP and RBF networks accordingly. Referring to Table 6, the MLP network concluded that the top five most essential contributing factors towards COVID-19 spread and death are the Total cases (100%), Percentage of death over population (19.9%), Average temperature (15.8%), Low temperature (5.9%), and Percentage of cases over population (5.4%). Whereas, the RBF network determined that the top six most important contributing factors towards COVID-19 spread and death are the Death (100%), Cases (99.5%), Population (99.2%), and 99.1% for all Total cases, Percentage of cases over population, and Percentage of death over population.

Table 5: MLP Independent Variable Importance

	Importance	Normalized Importance
cases	.008	1.2%
deaths	.006	0.9%
HIGHTEMPERATURE	.021	3.1%
LOWTEMPERATURE	.038	5.9%
AVERAGETEMPERATURE	.104	15.8%
population	.003	0.5%
TOTALCASES	.655	100.0%
PERCENTCASESPOPULATION	.036	5.4%
PERCENTDEATHPOPULATION	.131	19.9%

Table 6: RBF Independent Variable Importance

	Importance	Normalized Importance
cases	.149	99.5%
deaths	.150	100.0%
HIGHTEMPERATURE	.034	22.6%
LOWTEMPERATURE	.036	23.9%
AVERAGETEMPERATURE	.035	23.4%
population	.149	99.2%
TOTALCASES	.149	99.1%
PERCENTCASESPOPULATION	.149	99.1%
PERCENTDEATHPOPULATION	.149	99.1%

As previously discussed, the performance of the developed MLP and RBF networks were evaluated and investigated against a well-known empirical correlation using statistical and graphical error analyses which are SSE and RE.

By default, the rescaling method for covariates is Standardized. In this rescaling process, mean is subtracted from the values and the outcome is divided by the standard deviation. There are three more methods of rescaling which are Normalized, Adjusted normalized and None. Table 7, Table 8, Table 9 and Table 10 demonstrate the overall summary of RE and SSE for both MLP and RBF correspondingly (Figure 5).

Table 7: Relative Error of ANN MLP Models

Rescaling of Covariates	Optimization Algorithm	
	Scaled Conjugate Gradient	Gradient Descent
Standardized	0.498	3.208
Normalized	7.367	0.628
Adjusted Normalized	0.923	1.575
None	3.662	9.207

Table 8: SSE of ANN MLP Models

Rescaling of Covariates	Optimization Algorithm	
	Scaled Conjugate Gradient	Gradient Descent
Standardized	0.002	0.007
Normalized	0.050	0.002
Adjusted Normalized	0.002	0.004
None	0.016	0.043

Table 9: Relative Error of ANN RBF Models

Rescaling of Covariates	Radial Basis Neural Network Activation Function for Hidden Layer	
	Normalized Radial Basis Function	Ordinary Radial Basis Function
Standardized	1.169	0.971
Normalized	0.445	0.677
Adjusted Normalized	0.512	14458.309
None	1.453	12281.433

Table 10: SSE of ANN RBF Models

Rescaling of Covariates	Radial Basis Neural Network Activation Function for Hidden Layer	
	Normalized Radial Basis Function	Ordinary Radial Basis Function
Standardized	0.005	0.010
Normalized	0.003	0.003
Adjusted Normalized	0.005	1.050
None	0.008	1.164

Based on the Table 7 and 8, it can be monitored that MLP produced the best result in Standardized rescaling method, in which it returned the lowest values of SSE and RE of 0.498 and 0.002 as compared to the Normalized, Adjusted Normalized, and None.

Table 11: Configurations of ANN MLP Models

Rescaling of Covariates	Optimization Algorithm	
	Scaled Conjugate Gradient	Gradient Descent
Standardized	9-1-1	9-1-1
Normalized	9-1-1	9-1-1
Adjusted Normalized	9-1-1	9-1-1
None	9-1-1	9-1-1

Table 12: Configurations of ANN RBF Models

Rescaling of Covariates	Radial Basis Neural Network Activation Function for Hidden Layer	
	Normalized Radial Basis Function	Ordinary Radial Basis Function
Standardized	9-10-1	9-8-1
Normalized	9-7-1	9-3-1
Adjusted Normalized	9-7-1	9-5-1
None	9-4-1	9-10-1

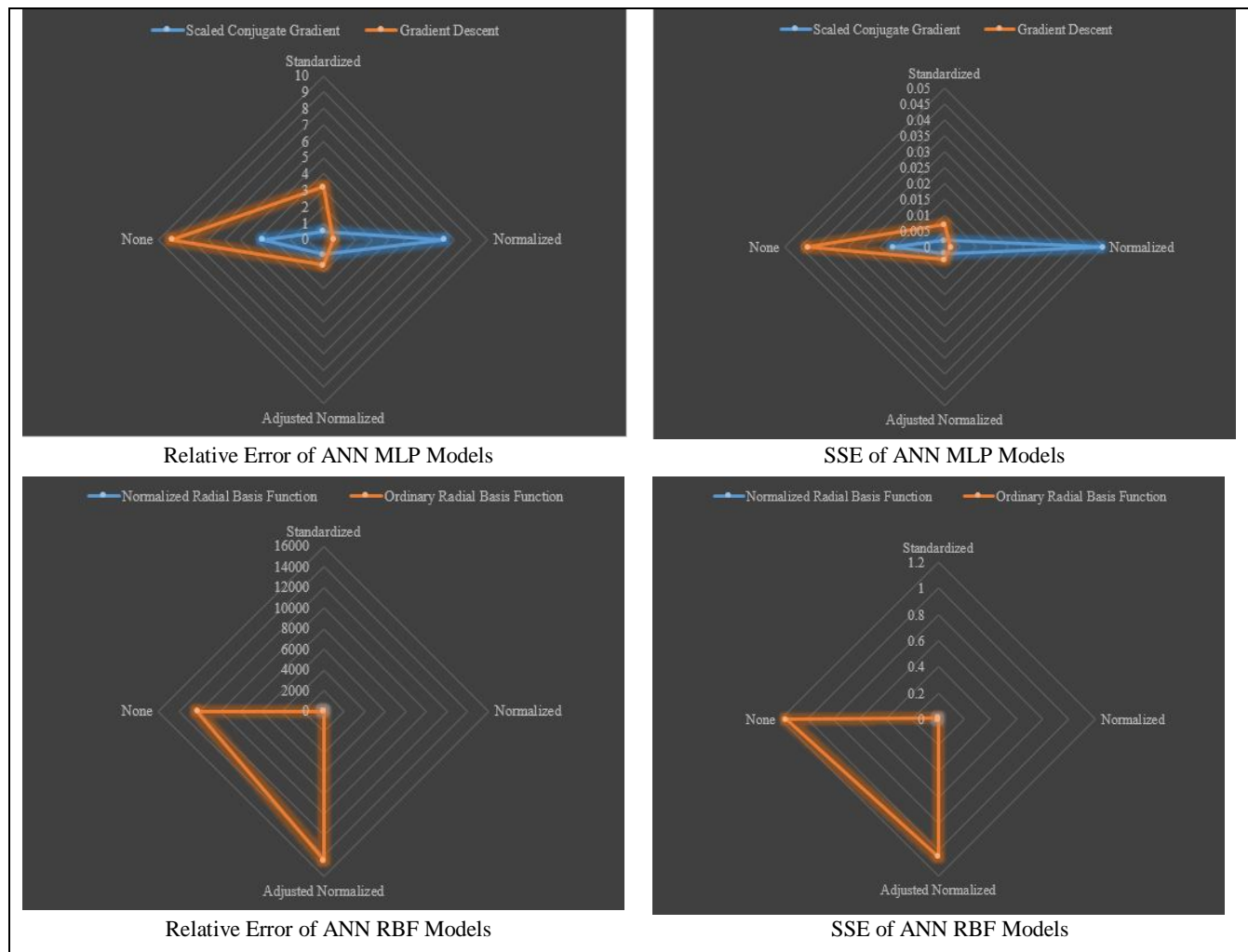


Figure 5: Overall summary of RE and SSE for both MLP and RBF models

Alternatively, the RBF is seen to compute the lowest RE and SSE values in the Normalized rescaling method which are 0.445 and 0.003, and are found to produce lower error rates than the MLP network as shown in Table 9 and Table 10. All configurations of both techniques can be referred in Table 11 and Table 12.

Conclusively, the performance evaluation indicated that both ANN models of MLP and RBF are effective in investigating the contributing factors of COVID-19 spread and death. However, the developed RBF exhibited higher accuracy and efficiency as compared to the proposed MLP model.

5. CONCLUSION

This paper presents a study on performance evaluation of Multilayer Perceptron (MLP) and a Radial Basis Function (RBF) networks in investigating the contributing factors for COVID-19 spread and death. A comparison was made by using a dataset of COVID-19 cases in 41 Asia countries during April 2020. There are nine contributing factors which acted as the covariates to the network such as Cases, Deaths,

High Temperature, Low Temperature, Population, Percentage of Cases over Population, and Percentage of Death over Population, Average Temperature, and Total Cases. The performance evaluation indicated that both ANN models of MLP and RBF are effective in investigating the contributing factors of COVID-19 spread and death. However, the developed RBF indicated a slightly better performance than the MLP.

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