

A Keystream-Based Affine Cipher for Dynamic Encryption

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ABSTRACT

In this paper, the use of a random seed is integrated to Affine cipher. The random seed is used to generate unique keystream values that dynamically changes the cipher's additive key for every character encrypted. The modification enables the cipher algorithm to produce ciphertext with no trace of repetitive character despite the advent of repetition of characters in the plaintext. Simulation results revealed that the proposed method produces more randomize ciphertext characters as against the traditional Affine cipher. The new method enhances the cipher's capability and complexity in masking plaintext which has paved the way to a more secure and dynamic data encryption.

Key words: Affine cipher, character repetition, cryptography, dynamic encryption, keystream

1. INTRODUCTION

There are numerous ways of securing sensitive information. One method is through encryption or the transformation of data into unintelligible format. Data is secured based on the cryptographic and cipher algorithm [1] used according to the type of data being hidden. Cipher [2] technology can be based on mathematical theories and some are based on classical calculations [3]. In this paper, the classical cipher called Affine cipher [2], [4]–[6] is modified to minimize the production of repetitive characters in the ciphertext. This is realized by introducing a random seed that produces unique encryption keys called keystream for the affine encryption and decryption function.

2. METHODOLOGY

2.1 Affine Cipher

The word affine is a term used to refer to the linear function $f(x) = (ax + b)$, where b is a nonzero value. In cryptography, the Affine cipher is a monoalphabetic substitution cipher based on the Caesar cipher and is defined by the formula $A_{j,d}$: $x \rightarrow y = A_{j,d}(x) = (jx + d) \bmod m$, where m is the range of alphabets, and j and d are the keys [7]. The values for j and m must be coprime so that decryption is possible through the equation $A_{j,d}(y) \equiv j^{-1}(y - d) \bmod m$, where j^{-1} is the inverse

modular multiplicative of modulo m that satisfies that equation $1 = aa^{-1} \bmod m$ [8]–[10].

Affine cipher works by mapping a set of alphabets to a range of integers. Using modular arithmetic, each plaintext character is transformed into an integer and that which is transformed into a ciphertext character [8], [9].

For instance, the plaintext UNNEEDED is encrypted using the traditional Affine cipher. First, each character is converted to its numerical equivalent according to its alphabetical index, such that A is 0 and Z is 25. The alphabets A to Z and their corresponding index values are presented in Table 1. Based on the given, the numerical equivalent of the plaintext UNNEEDED represented as x is 20 13 13 4 4 3 4 3, as shown in Table 2.

Table 1: Alphabet indices

A	B	C	D	E	F	G	H	I	J	K	L	M
0	1	2	3	4	5	6	7	8	9	10	11	12
N	O	P	Q	R	S	T	U	V	W	X	Y	Z
13	14	15	16	17	18	19	20	21	22	23	24	25

Table 2: Plaintext numerical equivalent

Plaintext	U	N	N	E	E	D	E	D
x	20	13	13	4	4	3	4	3

Given the affine encryption function $A_{j,d}(x) = (5x + 8) \bmod 26$ where the value 5 is coprime of the modulo, x is the numeric equivalent of the plaintext character, 8 is an arbitrary value for the number of shifts, and modulo 26 is the size of the alphabet, the plaintext is translated to 4 21 21 2 2 23 2 23 as presented in Table 3. These values are converted to ciphertext using the affine table as shown in Table 4.

Table 3: Encryption using Affine cipher

Plaintext	U	N	N	E	E	D	E	D
x	20	13	13	4	4	3	4	3
$(5x + 8) \bmod 26$	4	21	21	2	2	23	2	23
Ciphertext	E	V	V	C	C	X	C	X

The decryption process uses the equation $D(y) = 21(y - 8) \bmod 26$ where 21 is the modular multiplicative inverse a^{-1} of modulo 26, y is numeric equivalent of the ciphertext character, and 8 is the number of shifts. For instance, the ciphertext EVVCCXCX is translated as 4 21 21 2 2 23 2 23 and decrypted as UNNEEDED as presented in Table 5.

Table 4: Affine table based on $A_{j,d}(x) = (5x + 8) \bmod 26$

Alphabet	Index	$(5x+8) \bmod 26$	Ciphertext
A	0	8	I
B	1	13	N
C	2	18	S
D	3	23	X
E	4	2	C
F	5	7	H
G	6	12	M
H	7	17	R
I	8	22	W
J	9	1	B
K	10	6	G
L	11	11	L
M	12	16	Q
N	13	21	V
O	14	0	A
P	15	5	F
Q	16	10	K
R	17	15	P
S	18	20	U
T	19	25	Z
U	20	4	E
V	21	9	J
W	22	14	O
X	23	19	T
Y	24	24	Y
Z	25	3	D

Table 5: Decryption using Affine cipher

Ciphertext	E	V	V	C	C	X	C	X
y	4	21	21	2	2	23	2	23
$21(y-8) \bmod 26$	20	13	13	4	4	3	4	3
Plaintext	U	N	N	E	E	D	E	D

Like any other substitution ciphers, the Affine cipher produces obvious ciphertext patterns for plaintexts containing identical characters. As seen in Table 5, plaintext characters N and E appeared multiple times, thus, as soon as a certain repeating character is decrypted, the remaining identical characters can easily be substituted even without computation or cryptanalysis.

2.2 Proposed Cipher Process

The proposed process extends the capability of the standard Affine cipher by adding the digits 0 to 9 to the range of characters which can be processed, allowing a total of 36 possible plaintext and ciphertext values. The proposed method solves the weakness of the substitution cipher by ensuring that unique ciphertext values are produced and no obvious patterns appear for plaintext composed of identical characters such as AAAAAA or ABABABAB when encrypted. This is achieved by dynamically changing the cipher’s additive key for every character encrypted. The modified method uses a random seed value to produce a stream of unique encryption keys through the quadratic function $y = ax^2 + bx + c$, where b is the random seed value; c

is the character position; and a is the sum of x , b , and c . The keystream is used as the value d in the encryption and decryption functions.

The modified Affine cipher uses the equation $E(x) = (jx + d) \bmod 36$, where j must be a coprime of $\bmod 36$, x is the character index, and d is a value from the unique keystream. Decryption is done using the equation $D(y) = j^{-1}(y - d) \bmod 36$, where j^{-1} is the modular multiplicative inverse of $\bmod 36$, x is the character index, and d is a value from the unique keystream. The encryption and decryption processes of the modified Affine cipher is shown in Figures 1 and 2.

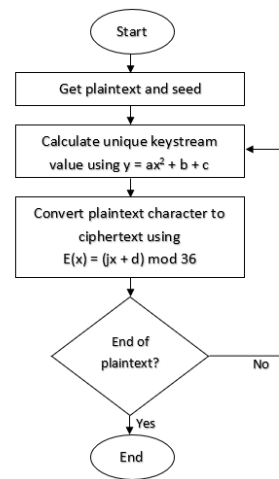


Figure 1: Modified Affine cipher encryption process

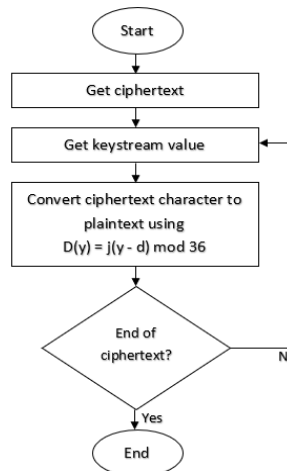


Figure 2: Modified Affine cipher decryption process

To perform encryption using the modified Affine cipher, the following detailed processes are executed:

- Identify the plaintext value and the random seed. The plaintext is any string composed of letters A to Z and digits 0 to 9, while the random seed can be any integer value. For example, the plaintext is MESSAGE and the seed is 12.
- Identify plaintext character index in the alphabet represented by x as shown in Table 6.

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